

Problem Set 6

1. Find a vector equation and parametric equations for the line through the point $(6, -5, 2)$ and parallel to the vector $\langle 1, 3, -\frac{2}{3} \rangle$.

2. Find parametric equations and symmetric equations for the line through the points $(1.0, 2.4, 4.6)$ and $(2.6, 1.2, 0.3)$.

3. Determine whether L_1 and L_2 are parallel, skew, or intersecting. If they intersect, find the point of intersection.

$$L_1: x = 3 + 2t, y = 4 - t, z = 1 + 3t$$

$$L_2: x = 1 + 4s, y = 3 - 2s, z = 4 + 5s$$

4. Find an equation of the plane through the point $(5, 3, 5)$ with a normal vector $2\mathbf{i} + \mathbf{j} - \mathbf{k}$.

5. Use intercepts to sketch the plane of $2x + 5y + z = 10$

6. Find the point at which the given line intersects the given plane.

$$x = 3 - t, y = 2 + t, z = 5t$$

$$x - y + 2z = 9$$

7. Determine whether the two planes are parallel, perpendicular, or neither. If neither, find the angle between them.

$$x + 4y - 3z = 1$$

$$-3x + 6y + 7z = 0$$

8. Find parametric equations for the line of intersection of the planes and find the angle between the planes:

$$x + y + z = 1$$

$$x + 2y + 2z = 1$$

9. Find the distance between the point $(1, -2, 4)$ and the plane $3x + 2y + 6z = 5$.

10. Find the distance between the two planes:

$$2x - 3y + z = 4$$

$$4x - 6y + 2z = 3$$